# APPENDIX I MATHEMATICS

The purpose of this mathematics appendix is twofold; first, it is a refresher for the Seabees who have encountered a time lapse between his or her schooling in mathematics; second, and more important, this section applies mathematics to the tasks that can not be accomplished without the correct use of mathematical equations.

#### **Linear Measurement**

Measurements are most often made in feet (ft) and inches (in). It is necessary that a Seabee know how to make computations involving feet and inches.

#### **Changing Inches to Feet and Inches**

To change inches to feet and inches, divide inches by 12. The quotient will be the number of feet, and the remainder will be inches.

## **Changing Feet and Inches to Inches**

To change feet and inches to inches, multiply the number of feet by 12 and add the number of inches. The results will be inches.

#### **Changing Inches to Feet in Decimal Form**

To change inches to feet in decimal form, divide the number of inches by 12 and carry the result to the required number of places.

#### **Changing Feet to Inches in Decimal Form**

To change feet in decimal form to inches, multiply the number of feet in decimal form by 12.

#### Addition of Feet and Inches

A Seabee often finds it necessary to combine or subtract certain dimensions which are given in feet and inches.

Arrange in columns of feet and inches and add separately. If the answer in the inches column is more than 12, change to feet and inches and combine feet.

#### **Subtraction of Feet and Inches**

Arrange in columns with the number to be subtracted below the other number. If the inches in the lower number are greater, borrow 1 foot (12 Inches) from the feet column in the upper number. Subtract as in any other problem.

#### **Multiplication of Feet and Inches**

Arrange in columns. Multiply each column by the required number. If the inches column is greater than 12, change to feet and inches then add to the number of feet.

#### **Division of Feet and Inches**

In dividing feet and inches by a given number, the problem should be reduced to inches unless the number of feet will divide by the number evenly.

To divide feet and inches by feet and inches, change to inches or feet (decimals).

#### **Angles**

When two lines are drawn in different directions from the same point, an angle is formed.

Angles are of four types:

- Right angle is a 90° angle.
- Acute angles are angles less than 90°.
- Obtuse angles are angles greater than 90°, but less than 180°.
- Reflex angle is an angle greater than 180°.

#### **Measurement of Angles**

Observe that two straight lines have been drawn to form four right angles. Refer to *Figure A-1*.

In order to have a way to measure angles, a system of angle-degrees has been established. Assume that each of the four right angles is divided into 90 equal angles. The measure of each is 1 angle degree; therefore, in the four right angles, there are 4 x 90°, or 360 angle degrees. For accurate measurement, degrees have been subdivided into minutes and minutes into seconds.

1 degree= 60 minutes (').

1 minute= 60 seconds (").

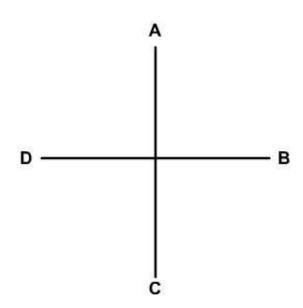


Figure A-1 — Right angles.

#### **Relationship of Angles**

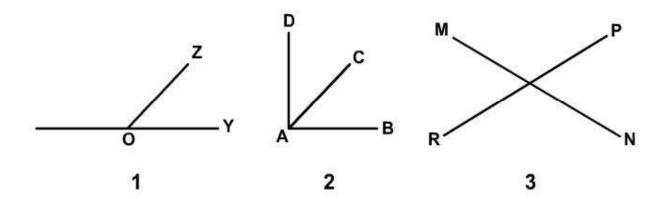


Figure A-2 — Relationship of angles.

- 1. ∠ZOY and ∠ZOX are supplementary angles and their total measure in degrees is equal to 180°. When one straight line meets another, two supplementary angles are formed. One is the supplement of the other. Refer to *Figure A-2, View* 1.
- 2. ∠DAC and ∠CAB are complementary angles and their total is a right angle or 90°. Refer to *Figure A-2*, *View 2*.

Two angles whose sum is 90° are said to be complementary, and one is the complement of the other.

3.  $\angle$ MOP and  $\angle$ RON are a pair of vertical angles and are equal. Refer to *Figure A-2*, *View 3*.

When two straight lines cross, two pairs of vertical angles are formed. Pairs of vertical angles are equal.

# **Bisecting Angles**

To bisect an angle merely means to divide the angle into two equal angles. This may be done by use of a compass.

#### **Perpendicular Lines**

Lines are said to be perpendicular when they form a right angle (90°).

#### **Parallel Lines**

Two lines are said to be parallel if they are equidistant (equally distant) at all points.

Facts about parallel lines:

Two straight lines lying in the same plane either intersect or are parallel.

Through a point there can be only one parallel drawn to a given line.

If two lines are perpendicular to the third, and in the same plane, they are parallel.

#### **Plane Shapes**

A plane shape is a portion of a plane bounded by straight or curved lines or a combination of the two.

The number of different types of plane shapes is infinite, but we are concerned with those which are of importance to you as a Seabee. We will cover the circle, triangle, quadrilateral, other polygons, and ellipses.

#### Circles

#### Definitions:

A CIRCLE is a closed curved line in which any point on the curved line is equidistant from a point called the center. (Circle O). Refer to *Figure A-3*.

A RADIUS is a line drawn from the center of a circle to a point on a circle. (As OA, OB, OX, and OY). Refer to *Figure A-3*.

A DIAMETER is a line drawn through the center of a circle with its ends lying on the circle. Refer to *Figure A-3*.

A DIAMETER is twice the length of a radius. (AB is a diameter of circle O) Refer to Figure A-3.

A CHORD is a line joining any two points lying on a circle. (CD is a chord of circle O.) Refer to *Figure A-3*.

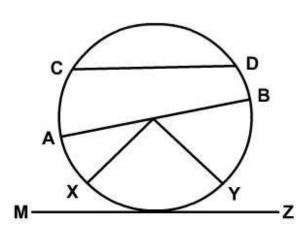


Figure A-3 — Circle.

An ARC is a portion of the closed curved lines which forms the circle. It is designated by CD. An arc is said to be subtended by a chord. Chord CD subtends arc CD. Refer to *Figure A-3*.

A TANGENT is a straight line which touches the circle at one and only one point. (Line MZ is a tangent to circle O.) Refer to *Figure A-3*.

A CENTRAL ANGLE is an angle whose vertex is the center of a circle and whose side are radii of the circle. (As XOY, YOA, and XOB.) Refer to *Figure A-3*.

CONCENTRIC CIRCLES are circles having the same center and having different radii.

The CIRCUMFERENCE of a circle is the distance around the circle. It is the distance on the curve from C to A to X to Y to B to D and back to C. Refer to *Figure A-3*.

#### Triangles

A triangle is a plane shape having 3 sides. Its name is derived from its three (tri) angles.

- 1. Equilateral all sides are equal, all angles are equal, and all angles are 60°. Refer to *Figure A-4*.
- 2. Isosceles two sides are equal and two angles are equal. Refer to Figure A-4.
- 3. Scalene all sides are unequal and all angles are unequal. Refer to *Figure A-4*.
- 4. Right one right angle is present. Refer to *Figure A-4*.

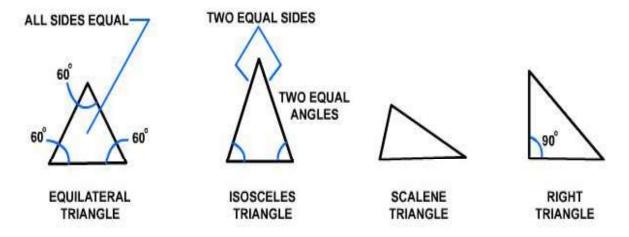


Figure A-4 — Types of triangles.

#### **Altitudes and Medians**

The altitude and median of a triangle are not the same; the difference is pointed out in the following definitions:

- 1. The altitude of a triangle is a line drawn from the vertex, perpendicular to the base. Refer to *Figure A-5*. *View 1*.
- 2. The median of a triangle is a line drawn from the vertex to the midpoint of the base. Refer to *Figure A-5*, *View 2*.

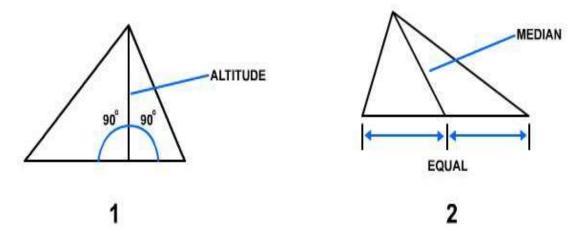


Figure A-5 — Altitude and median of a triangle.

### **Construction of Triangles**

There are many ways to construct a triangle, depending upon what measurements are known to you. The following definitions will assist you.

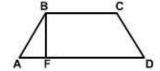
- 1. A triangle may be constructed if the lengths of three sides are known.
- 2. A triangle may be constructed if two sides and the included angle (angle between the sides) are known.
- 3. A triangle may be constructed if two angles and the included side are given.
- 4. A right triangle may be constructed if the two sides adjacent to the right angle are known.
- 5. A right triangle may be constructed by making the sides 3, 4, and 5 inches or multiples or fractions thereof.

#### **Quadrilaterals**

A quadrilateral is a four-sided plane shape. There are many types, but only the trapezoid, parallelogram, rectangle, and square are described here.

Trapezoid is a quadrilateral having only two sides parallel. If the other two sides are equal, it is an isosceles trapezoid. BF is the altitude of the trapezoid. See *Figure A-6*.

Parallelogram is a quadrilateral having opposite sides parallel. Refer to *Figure A-7*.



- 1. AB is parallel to CD.
- 2. AC is parallel to BD.
- 3. AD and CB are diagonals.
- 4. Diagonals bisect each other so CO = OB and AO = OD.
- 5. Opposite angles are equal. ACD = DBA and CAB = BDC.
- 6. If two sides of a quadrilateral are equal and parallel, the figure is a parallelogram.
- 7. A parallelogram may be constructed if two adjoining sides and one angle are known.

Rectangle is a parallelogram having one right angle. Refer to *Figure A-8*.

- 1. ABCD is a parallelogram having one right angle. This, of course, makes all angles right angles.
- 2. AC and BD are diagonals.
- 3. O is the midpoint of AC and BD and OB = OC = OD = OA.
- 4. O is equidistant from BC and AD and is also equidistant from AB and CD.
- 5. A rectangle may be constructed if two adjoining sides are known

Square is a rectangle having its adjoining sides equal. Refer to *Figure A-9*.

Figure A-6 — Trapezoid.

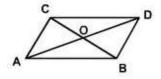


Figure A-7 — Parallelogram.

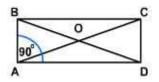


Figure A-8 — Rectangle.

- 1. ABCD is a square.
- 2. AC and BD are diagonals.
- 3. O is the geometric center of the square. AO = OC = OB = OD.
- 4. O is equidistant from all sides.
- 5. A square may be constructed if one side is known.

# **Polygons**

A polygon is a many-sided plane shape. It is said to be regular if all sides are equal and irregular when they are not. Only regular polygons are described here.

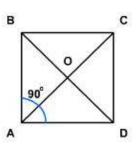


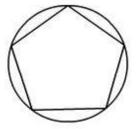
Figure A-9 — Square.

Triangles and quadrilaterals fit the description of a polygon and have been covered previously. Three other types of regular polygons are shown in *Figure A-10*. Each one is inscribed in a circle. This means that all vertices of the polygon lie on the circumference of the circle.

Note that the sides of each of the inscribed polygons are actually equal chords of the circumscribed circle. Since equal chords subtend equal arcs, by dividing the circumference into an equal number of arcs, a regular polygon may be inscribed in a circle. Also note that the central angles are equal because they intercept equal arcs. This gives a basic rule for the construction of regular polygons inscribed in a circle as follows:

To inscribe a regular polygon in a circle, create equal chords of the circle by dividing the circumference into equal arcs or by dividing the circle into equal central angles.

Dividing a circle into a given number of parts has been discussed, so construction should be no problem. Since there are 360 degrees around the center of the circle, you should have no problem in determining the number of degrees to make each equal central angle.



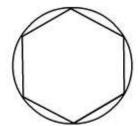




Figure A-10 — Types of polygons.

### **Methods for Constructing Polygons**

The three methods for constructing polygons described here are the pentagon, hexagon, and octagon.

The Pentagon is a developed by dividing the circumference into 5 equal parts.

The Hexagon is developed by dividing the circumference into 6 equal parts.

The Octagon method has been developed by creating central angles of 90° to divide a circle into 4 parts and bisecting each arc to divide the circumference into 8 equal parts.

### **Ellipses**

An ellipse is a plane shape generated by point P, moving in such a manner that the sum of its distances from two points,  $F_1$  and  $F_2$ , is constant. Refer to *Figure A-11*.

$$BF_1 + PF_2 = C = (a constant)$$

AE is the major axis.

BD is the minor axis.

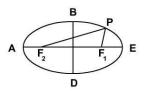


Figure A-11 — Ellipses.

#### **Perimeters and Circumferences**

Perimeter and circumference have the same meaning; that is, the distance around. Generally, circumference is applied to a circular object and perimeter to an object bounded by straight lines.

### Perimeter of a Polygon

The perimeter of a triangle, quadrilateral, or any other polygon is actually the sum of the sides.

#### Circumference of a Circle

Definition of Pi: Mathematics have established that the relationship of the circumference to the diameter of a circle is a constant called Pi and written as  $\pi$ . The numerical value of this constant is approximately 3.141592653. For our purposes 3.1416 or simply 3.14 will suffice.

The formula for the circumference of a circle is  $C = 2\pi D$  where C is the circumference and D is the diameter since D = 2R where R is the radius, the formula may be written as  $C = 2\pi R$ .

#### **Areas**

All areas are measured in squares.

The area of a square is the product of two of its sides and since both sides are equal, it may be said to be square of its side.

#### NOTE

The area of any plane surface is the measure of the number of squares contained in the object. The unit of measurement is the square of the unit which measures the sides of the square.

### Area of Rectangle

 $A = L \times W$ 

Where:

A = area of a rectangle

L = length of a rectangle

W = width of a rectangle

#### Area of a Cross Section

The cross section of an object is a plane figure established by a plane cutting the object at right angles to its axis. The area of this cross section will be the area of the plane figure produced by this cut.

The area of the cross section is L x W.

The most common units are square inches, square feet, square yards and in roofing, "squares."

1 square foot = 144 square inches

1 square yard = 9 square feet

1 square of roofing = 100 square feet

#### **Common Conversions**

- 1. To convert square inches to square feet, divide square inches by 144.
- 2. To convert square feet to square inches, multiply by 144.
- 3. To convert square feet to square yards, divide by 9.
- 4. To convert square yards to square feet, multiply by 9.
- 5. To convert square feet to squares, divide by 100.

#### **Conversion of Units of Cubic Measure**

It is often necessary to convert from one cubic measure to another. The conversion factors used are as follows:

- 1. 1 cubic foot = 1,728 cubic inches
- 2. 1 cubic yard = 27 cubic feet
- 3. 1 cubic foot = 7.48 US gallons (liquid measure)
- 4. 1 us gallon (liquid measure) = 231 cubic inches
- 5. 1 bushel (dry measure) = 2,150.42 cubic inches

#### Area of a Circle

The formula for the area of a circle is:

 $A = \pi r^2$ 

Where:

A = area of circle

r = radius of circle

 $\pi = 3.1416$ 

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Since r = d/2 where d is the diameter of a circle, the formula for the area of a circle in terms of its diameter is:

$$A = \pi(\frac{d^2}{2}) = \frac{\pi d^2}{4}$$

#### **Geometric Solids**

In describing plane shapes, you use only two dimensions: width and length; there is no thickness. By adding the third dimension, you describe a solid object.

Consider the solids described below.

Prism - is a figure whose two bases are polygons, alike in size and shape, lying in parallel planes and whose lateral edges connect corresponding vertices and are parallel and equal in length. A prism is a right prism if the lateral edge is perpendicular the base. The altitude of a prism is the perpendicular distance between the bases.

Cone - is a figure generated by a line moving in such a manner that one end stays fixed at a point called the "vertex." The line constantly touches a plane curve which is the base of the cone. A cone is a circular cone if its base is a circle. A circular cone is a right circular cone if the line generating it is constant in length. The altitude of a cone is the length of a perpendicular to the plane of the base drawn from the vertex.

Pyramid - is a figure whose base is a plane shape bounded by straight lines and whose sides are triangular plane shapes connecting the vertex and a line of the base. A regular pyramid is one whose base is a regular polygon and whose vertex lays on a perpendicular to the base at its center. The altitude of a pyramid is the length of a perpendicular to the plane of the base drawn from the vertex.

Circular Cylinder - is a figure whose bases are circles lying in parallel planes connected by a curved lateral surface. A right circular cylinder is one whose lateral surface is perpendicular to the base. The altitude of a circular cylinder is the perpendicular distance between the planes of the two bases.

#### **Measurement of Volume**

Volume is measured in terms of cubes.

#### **Common Volume Formulas**

All factors in the formulas must be in the same linear units. As an example, one term could not be expressed in feet while other terms are in inches.

#### **Volume of a Rectangular Prism**

$$V = L \times W \times H$$

Where:

V = Volume in cubic inches

W = Width of the base in linear units

L = Length of base in linear units

H = Altitude of the prism in linear units

#### Volume of a Cone

$$V = \frac{Axh}{3}$$

Or

$$V = \frac{\pi r^2 h}{3}$$

Or

$$V = \frac{\pi d^2 h}{12}$$

Where:

V= Volume of a cone in cubic units

A = Area of the base in square units

h = Altitude of a cone in linear units

r = Radius of the base

d = Diameter of the base

# Volume of a Pyramid

$$V = \frac{Ah}{3}$$

Where:

V = Volume in cubic units

A = Area of base in square units

h = Altitude in linear units

# Volume of a Cylinder

$$V = Ah$$

Or

$$V = \pi r^2 h$$

Or

$$V = \frac{\pi d^2 h}{4}$$

Where:

V = Volume in cubic units

A = Area of the base in square units

h = Altitude in linear units

r = Radius of the base

d = Diameter of the base

### Volume of the Frustum of a Right Circular Cone

The frustum of a cone is formed when a plane is passed parallel to the base of the cone. The frustum is the portion below the plane. The altitude of the frustum is the perpendicular distance between the bases.

$$V = 1/3 \pi h (r^2 + R^2 + Rr)$$

Where:

h = Altitude in linear units

r = Radius of the upper base in linear units

R = Radius of the lower base in linear units

### Volume of a Frustum of a Regular Pyramid

A frustum of a pyramid is formed when a plane is passed parallel to the base of the pyramid. The frustum is the portion below the plane. The altitude is the perpendicular distance between the bases.

$$V = 1/3h (B + b + \sqrt{Bb})$$

Where:

V = Volume of the frustum in cubic units

h = Altitude in linear units

B = Area of the lower base in square units

b = Area of the upper base in square units

#### **Ratio**

The ratio of one number to another is the quotient of the first, divided by the second. This is often expressed as a:b, which is read as the ratio of a to b. More commonly, this expressed as the fraction a/b.

Ratio has no meaning unless both terms are expressed in the same unit by measurement.

#### **Percentage**

Percentage (%) is a way of expressing the relationship of one number to another. In reality, percentage is a ratio expressed as a fraction in which the denominator is always one hundred.

# **Proportion**

Proportion is a statement of two ratios which are equal.

Example: 1/3 = 5/15 or 1:3 = 5:15

Solving proportions is done by cross multiplying.

Example:  $\frac{a}{b} = \frac{c}{d} = a \times d = b \times c$ 

# **Law of Pythagoras**

The Law of Pythagoras is the square of the hypotenuse of a right triangle equals the sum of the two legs. It is expressed by the formula  $a^2 + b^2 = c^2$ .

Right Triangle: a triangle having one right angle

Hypotenuse: The hypotenuse of a right triangle is the side opposite the right angle

Leg: The leg of a right triangle is a side opposite and acute angle of a right triangle.

#### **METRIC CONVERSION TABLES**

# **Length Conversion**

When You Know:	You Can Find:	If You Multiply By:
inches	millimeters	25.4
inches	centimeters	2.54
feet	centimeters	30
feet	meters	0.3
yards	centimeters	90
yards	meters	0.9
miles	kilometers	1.6
miles	meters	1609
millimeters	inches	0.04
centimeters	inches	0.4
centimeters	feet	0.0328
meters	feet	3.3
centimeters	yards	0.0109
meters	yards	1.1
meters	miles	0.000621
kilometers	miles	0.6
meters	nautical miles	0.00054
nautical miles	meters	1852

# Weight Conversion

When You Know:	You Can Find:	If You Multiply By:
ounces	grams	28.3
pounds	kilograms	0.45
short tons	megagrams	0.9
(2000 lbs)	(metric tons)	
grams	ounces	0.0353
kilograms	pounds	2.2
megagrams	short tons	1.1
(metric tons)	(2000 lbs)	

# **Temperature Conversion**

When You Know:	You Can Find:	If You Multiply By:
Degrees Fahrenheit	Degree Celsius	Subtract 32 then multiply by 5/9
Degrees Celsius	Degree Fahrenheit	Multiply by 9/5 then add 32
Degrees Celsius	Kelvins	Add 273.15°

# **Volume Conversion**

When You Know:	You Can Find:	If You Multiply By:
teaspoons	milliters	5
tablespoons	milliters	1 5
fluid ounces	milliters	3 0
cups	liters	0.24
pints	liters	0.47
quarts	liters	0.95
gallons	liters	3.8
milliters	teaspoons	0.2
milliters	tablespoons	0.067
milliters	fluid ounces	0.034
liters	cups	4.2
liters	pints	2.1
liters	quarts	1.06
liters	gallons	0.26
cubic feet	cubic meters	0.028
cubic yards	cubic meters	0.765
cubic meters	cubic feet	35.3
cubic meters	cubic yards	1.31

# **Area Conversions**

When You Know:	You Can Find:	If You Multiply By:
Square inches	Square centimeters	6.45
Square inches	Square meters	0.000 6
Square feet	Square centimeters	929
Square feet	Square meters	0.0929
Square yards	Square centimeters	8.360
Square yards	Square meters	0.836
Square miles	Square kilometers	2.6
Square centimeters	Square inches	0.155
Square meters	Square inches	1550
Square centimeters	Square feet	0.001
Square meters	Square feet	10.8
Square centimeters	Square yards	0.00012
Square meters	Square yards	1.2
Square kilometers	Square miles	0.4

Table A-1 — Decimal Equivalents.

Fraction	16 <sup>th</sup>	32 <sup>nd</sup>	64 <sup>th</sup>	Decimal	Fraction	16 <sup>th</sup>	32 <sup>nd</sup>	64 <sup>th</sup>	Decimal
			1	.015625				33	.515625
		1	2	.03125			17	34	.53125
			3	.046875				35	.54875
	1	2	4	.0625		9	18	36	.5625
			5	.078125				37	.578125
		3	6	.09375			19	38	.59375
			7	.109375				39	.609375
1/8	2	4	8	.125	5/8	10	20	40	.625
			9	.140625				41	.640625
		5	10	.15625			21	42	.65625
			11	.171875				43	.671875
	3	6	12	.1875		11	22	44	.6875
			13	.203125				45	.703125
		7	14	.21875	.21875		23	46	.71875
			15	.234375	.234375 47		47	.734375	
1/4	4	8	16	.25	.25 3/4 12		24	48	.75
			17	.265625	5625			49	.765625
		9	18	.28125			25	50	.78125
			19	.296875			51	.796875	
	5	10	20	.3125	125 13 26		52	.8125	
			21	.328125	25		53	.818225	
		11	22	.34375	375 27 54		54	.84375	
			23	.359375				55	.859375
3/8	6	12	24	.375	7/8	14	28	56	.875
			25	.390623				57	.890625
		13	26	.40625			29	58	.90625
			27	.421875				59	.921875
	7	14	28	.4375		15	30	60	.9375
			29	.453125				61	.953125
		15	30	.46875			31	62	.96875
			31	.484375				63	.984375
1/2	8	16	32	.5	1	16	32	64	1.0

Table A-2 — Metric measures of length.

10 millimeters	=	1 centimeter (cm)	
10 centimeters	=	1 decimeter (dm)	
10 decimeters	ers = 1 meter (m)		
10 meters	=	1 decameter (dkm)	
10 decameters	=	1 hectometer (hm)	
10 hectometers	=	1 kilometer (km)	

Table A-3 — Conversion of inches to millimeters.

Inches	Millimeters	Inches	Millimeters	Inches	Millimeters	Inches	Millimeters
1	25.4	26	660.4	51	1295.4	76	1930.4
2	50.8	27	685.8	52	1320.8	77	1955.8
3	76.2	28	711.2	53	1346.2	78	1981.2
4	101.6	29	736.6	54	1371.6	79	2006.6
5	127	30	762	55	1397	80	2032
6	152.4	31	787.4	56	1422.4	81	2057.4
7	177.8	32	812.8	57	1447.8	82	2082.8
8	203.2	33	838.2	58	1473.2	83	2108.2
9	228.6	34	863.6	59	1498.6	84	2133.6
10	254	35	889	60	1524	85	2159
11	279.4	36	914.4	61	1549.4	86	2184.4
12	304.8	37	939.8	62	1574.8	87	2209.8
13	330.2	38	965.2	63	1600.2	88	2235.2
14	355.6	39	990.6	64	1625.6	89	2260.6
15	381	40	1016	65	1651	90	2286
16	406.4	41	1041.4	66	1676.4	91	2311.4
17	431.8	42	1066.8	67	1701.8	92	2336.8
18	457.2	43	1092.2	68	1727.2	93	2362.2
19	482.6	44	1117.6	69	1752.6	94	2387.6
20	508	45	1143	70	1778	95	2413
21	533.4	46	1168.4	71	1803.4	96	2438.4
22	558.8	47	1193.8	72	1828.8	97	2463.8
23	584.2	48	1219.2	73	1854.2	98	2489.2
24	609.6	49	1244.6	74	1879.6	99	2514.6
25	635	50	1270	75	1905	100	2540

Table A-4 — Conversions of fractions and decimals to millimeters.

Table A-4 — Conversions of fractions and decimals to minimeters.							
Fraction of inch (64ths)	Decimal of Inch	Millimeters	Fraction of inch (64ths)	Decimal of Inch	Millimeters		
1	.015625	.3968	33	.515625	13.0966		
2	.03125	.7937	34	53125	13.4934		
3	.046875	1.1906			13.8903		
4 (1/16")	.0625	1.5875	36	.546875 .5625	14.2872		
5	.078125	1.9843	1.9843 37		14.6841		
6	.09375	2.3812	38	.59375	15.0809		
7	.109375	2.7780	39	.609375	15.4778		
8 (1/8")	.125	3.1749	40 (5/8")	.625	15.8747		
9	.140625	3.5817	41	.640625	16.2715		
10	.15625	3.9686	42	.65625	16.6684		
11	.171875	4.3655	43	.671875	17.0653		
12	.1875	4.7624	44	.6875	17.4621		
13	.203125	5.1592	45	.703125	17.8590		
14	.21875	5.5561	46	.71875	18.2559		
15	.234375	5.9530	47	.734375	18.6527		
16 (1/4")	.25	6.3498	48 (3/4")	.75	19.0496		
17	.265625	6.7467	49	.765625	19.4465		
18	.28125	7.1436	50	.78125	19.8433		
19	.296875	7.5404	51	.796875	20.2402		
20	.3125	7.9373	52	.8125	20.6371		
21	.328125	8.3342	53	.818225	21.0339		
22	.34375	8.7310	54	.84375	21.4308		
23	.359375	9.1279	55	.859375	21.8277		
24 (3/8")	.375	9.5248	56 (7/8")	.875	22.2245		
25	.390623	9.9216	57	.890625	22.6214		
26	40625	10.3185	58	.90625	23.0183		
27	.421875	10.7154	59	.921875	23.4151		
28	4375	11.1122	60	.9375	23.8120		
29	.453125	11.5091	61	.953125	24.2089		
30	.46875	11.9060	62	.96875	24.6057		
31	.484375	12.3029	63	.984375	25.0026		
32 (1/2")	.5	12.6997	64 (1")	1.0	25.3995		

**Table A-5 Conversions of measurements.** 

Conversion Chart for Measurement								
inahaa		CONV	ersion	Jilai ( 10	ivieasui	ement		
inches							. 1	centimeters
Cm							inches	
Feet						meters		
Meters					feet			
Yards				meters				
Meters			yards					
Miles		kilometers						
km	miles							
1	0.62	1.61	1.09	0.91	3.28	0.30	0.39	2.54
2	1.21	3.22	2.19	1.83	6.56	0.61	0.79	5.08
3	1.86	4.83	3.28	2.74	9.81	0.91	1.18	7.62
4	2.49	6.44	4.37	3.66	13.12	1.22	1.57	10.16
5	3.11	8.05	5.47	4.57	16.40	1.52	1.97	12.70
6	3.73	9.66	6.56	5.49	19.68	1.83	2.36	15.24
7	4.35	11.27	7.66	6.4	22.97	2.13	2.76	17.78
8	4.97	12.87	8.75	7.32	26.25	2.44	3.15	20.32
9	5.59	14.48	9.84	8.23	29.53	2.74	3.54	22.86
10	6.21	16.09	10.94	9.14	32.81	3.05	3.93	25.40
12	7.46	19.31	13.12	10.97	39.37	3.66	4.72	30.48
20	12.43	32.19	21.87	18.29	65.62	6.10	7.87	50.80
24	14.91	38.62	26.25	21.95	78.74	7.32	9.45	60.96
30	18.64	48.28	32.81	27.43	98.42	9.14	11.81	76.20
36	22.37	57.94	39.37	32.92	118.11	10.97	14.17	91.44
40	24.37	64.37	43.74	36.58	131.23	12.19	15.75	101.60
48	29.83	77.25	52.49	43.89	157.48	14.63	18.90	121.92
50	31.07	80.47	54.68	45.72	164.04	15.24	19.68	127.00
60	37.28	96.56	65.62	54.86	196.85	18.29	23.62	152.40
70	43.50	112.65	76.55	64	229.66	21.34	27.56	177.80
72	44.74	115.87	78.74	65.84	236.22	21.95	28.35	182.88

Table A-6 — Cubic conversion chart.

Cubic Conversion Chart							
Cubic Meters				Cubic Feet	Cubic Yard		
Cubic Yard			Cubic Meters				
Cubic Feet		Cubic Meters					
Cubic	Cubic						
Inches	Centimeters						
1	16.39	0.028	0.76	35.3	1.31		
2	32.77	0.057	1.53	70.6	2.62		
3	49.16	0.085	2.29	105.9	3.92		
4	65.55	0.113	3.06	141.3	5.23		
5	81.94	0.142	3.82	176.6	6.54		
6	98.32	0.170	4.59	211.9	7.85		
7	114.71	0.198	5.35	247.2	9.16		
8	131.10	0.227	6.12	282.5	10.46		
9	147.48	0.255	6.88	317.8	11.77		
10	163.87	0.283	7.65	353.1	13.07		
20	327.74	0.566	15.29	706.3	26.16		
30	491.61	0.850	29.94	1059.4	39.24		
40	655.48	1.133	30.58	1412.6	52.32		
50	819.35	1.416	38.23	1765.7	65.40		
60	983.22	1.700	45.87	2118.9	78.48		
70	1174.09	1.982	53.52	2472.0	91.56		
80	1310.96	2.265	61.16	2825.2	104.63		
90	1474.84	2.548	68.81	3178.3	117.71		
100	1638.71	2.832	76.46	3531.4	130.79		

Example: 3 cu. Yd = 2.29 cu. M

Volume: The cubic meter is the only common dimension used for measuring the volume of solids in the metric system.

Table A-7 — Gallon and liter conversion chart.

Gallon	Liter	Gallon	Liter	Gallon	Liter
.1	.38	1	3.79	10	37.85
.2	.76	2	7.57	20	57.71
.3	1.14	3	11.36	30	113.56
.4	1.51	4	15.14	40	151.42
.5	1.89	5	18.93	50	189.27
.6	2.27	6	22.71	60	227.12
.7	2.65	7	26.50	70	264.98
.8	3.03	8	30.28	80	302.83
.9	3.41	9	34.07	90	340.69

**NOTE:** 1 us Gallon = 3.785412 Liters 100 us Gallons = 378.5412 Liters

Table A-8 — Weight conversion chart.

lable A-8 — Weight conversion chart.							
Weight Conversion Chart							
Ounces						Grams	
Grams					Ounces		
Pounds				Kilograms			
Kilograms			Pounds				
Short Ton		Metric					
Short ron		Ton					
Metric	Short						
Ton	Ton						
1	1.10	0.91	2.20	0.45	0.04	28.1	
2	2.20	1.81	4.41	0.91	0.07	56.7	
3	3.31	2.72	6.61	1.36	0.11	85.0	
4	4.41	3.63	8.82	1.81	0.14	113.4	
5	5.51	4.54	11.02	2.67	0.18	141.8	
6	6.61	5.44	13.23	2.72	0.21	170.1	
7	7.72	6.35	15.43	3.18	0.25	198.4	
8	8.82	7.26	17.64	3.63	0.28	226.8	
9	9.92	8.16	19.81	4.08	0.32	255.2	
10	11.02	9.07	22.05	4.54	0.35	283.5	
16	17.63	14.51	35.27	7.25	0.56	453.6	
20	22.05	18.14	44.09	9.07	0.71	567.0	
30	33.07	27.22	66.14	13.61	1.06	850.5	
40	44.09	36.29	88.14	18.14	1.41	1134.0	
50	55.12	45.36	110.23	22.68	1.76	1417.5	
60	66.14	54.43	132.28	27.22	2.12	1701.0	
70	77.16	63.50	154.32	31.75	2.17	1981.5	
80	88.18	72.57	176.37	36.29	2.82	2268.0	
90	99.21	81.65	198.42	40.82	3.17	2551.5	
100	110.20	90.72	220.46	45.36	3.53	2835.0	
<b>NOTE:</b> 1 pound = 0.4535925 KG; 1 US Short Ton = 2,000 pounds; and 1 Metric Ton = 1,000 KG							

#### **FORMULAS**

#### **Conversion Factors and Constants**

$$\pi = 3.14$$

$$2\pi = 6.28$$

$$\pi^2 = 9.87$$

$$(2\pi)^2 = 39.5$$

$$\varepsilon$$
 = 2.718

$$\sqrt{2} = 1.414$$

$$\sqrt{3} = 1.732$$

# **Sinusoidal Voltages and Currents**

Effective Value = 0.707 x Peak Value

Average Value = 0.637 x Peak Value

Peak Value = 1.414 x Effective Value

Effective Value = 1.11 x Average Value

Peak Value = 1.57 x Average Value

Average Value = 0.9 x Effective Value

# **Temperature**

$$(F \text{ to } C) C = 5/9 (F - 32)$$

$$(C \text{ to } F) F = 9/5 C = 32$$

$$(C \text{ to } K) K = C + 73$$

#### **Power**

1 kilowatt = 1.341 horsepower

1 horsepower = 746 watts

# **Trigonometric Formulas**

$$\sin A = \frac{a}{c} = \frac{Opposite\ Side}{Hypotenuse}$$

$$\cos A = \frac{b}{c} = \frac{Adjacent\ Side}{Hypotenuse}$$

$$\tan A = \frac{a}{b} = \frac{Opposite\ Side}{Adjacent\ Side}$$

$$\cot A = \frac{b}{a} = \frac{Adjacent \ Side}{Opposite \ Side}$$

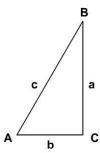


Figure A-12 — Trapezoid.

#### **Ohm's Law-Direct Current**

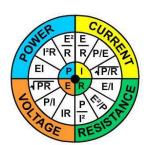


Figure A-13 — Direct Current.

# **Ohm's Law- Alternating Current**

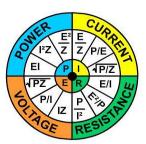


Figure A-14 — Alternating Current.

# Speed vs. Poles Formulas

$$F = \frac{NP}{120} \quad N = \frac{F \ 120}{P} \quad P = \frac{F \ 120}{N}$$

F = frequency

N= speed of rotation

P = number of poles

120 = time constant

Power Factor

$$PF = \frac{\text{actual power}}{\text{apparent power}} = \frac{\text{watts}}{\text{volts x amperes}} = \frac{\text{kW}}{\text{kVA}} = \frac{\text{R}}{\text{Z}}$$

### Single-Phase Circuits

$$kVA = \frac{EI}{1,000} = \frac{kW}{PF} kW = kVA \times PF$$

$$I = \frac{P}{E \times PF} E = \frac{P}{I \times PF} PF = \frac{P}{E \times PF}$$

$$P = E \times I \times PF$$

# Three-Phase Circuits, Balanced Wye

I phase = I line

$$E_{\scriptscriptstyle L} = \sqrt{3} \; E_{\scriptscriptstyle P} = 1.73 \, E_{\scriptscriptstyle P}$$

$$E_{P} = \frac{E_{L}}{\sqrt{3}} = 0.577 E_{L}$$

### **Two-Phase Circuits**

$$I = \frac{P}{2 \times E \times PF} E = \frac{P}{2 \times I \times PF} PF = \frac{P}{E \times I}$$

$$I = \frac{P}{E \times PF} E = \frac{P}{I \times PF} PF = \frac{P}{E \times I}$$
  $kVA = \frac{2 \times E \times I}{1,000} \frac{kW}{PF} kW = kVA \times PF$ 

$$P = 2 \times E \times I \times PF$$

# Three-Phase Circuits, Balanced Wye

E phase = E line

$$I_{L} = \sqrt{3} I_{D} = 1.73 I_{D}$$

$$I_{P} = \frac{I_{L}}{\sqrt{3}} = 0.577 I_{L}$$

# Power: Three-Phase Balanced Wye or Delta Circuits

$$P = 1.732 \times E \times I \times PF \quad VA = 1.732 \times E \times I$$

$$\mathsf{E} = \frac{P}{PF \ x \ 1.73 \ x \ I} = \frac{0.577 \ x \ P}{PF \ x \ I}$$

$$I = \frac{P}{PF \times 1.73 \times E} = \frac{0.577 \times P}{PF \times E}$$

$$PF = \frac{P}{PF \times 1.73 \times E} = \frac{0.577 \times P}{I \times E}$$

```
VA = apparent power (volt-amperes)
P = actual power (watts)
E = line voltage (volts)
I = line current (amperes)
                           WEIGHTS AND MEASURES
                                    Dry Measure
2 \text{ cups} = 1 \text{ quart (pt)}
2 pints = 1 quart (pt)
4 quarts = 1 gallon (gal)
8 quarts = 1 peck (pk)
4 pecks = 1 bushel (bu)
                                   <u>Liquid Measure</u>
3 teaspoons (tsp) = 1 tablespoon (tbsp)
16 tablespoons = 1 cup
2 \text{ cups} = 1 \text{ pint}
16 fluid ounces (oz) = 1 pint
2 pints = 1 quart
4 quarts = 1 gallon
31.5 gallons = 1 barrel (bbl)
231 cubic inches = 1 gallon
7.48 gallons = 1 cubic foot (cu ft)
                                       Weight
16 ounces = 1 pound (lb)
2,000 pounds = 1 short ton
2,240 pounds = 1 long ton
                                      <u>Distance</u>
```

12 inches = 1 foot (ft)
3 feet = 1 yard (yd)
5-1/2 yards = 1 rod (rd)
16-1/2 feet = 1 rod
1,760 yards = 1 statute mile (mi)
5,280 feet = 1 statute mile

#### Area

144 square inches = 1 square foot (sq ft)

9 square feet = 1 square yd (sq yd)

30- 1/4 square yards = 1 square rod

160 square rods = 1 acre (A)

640 acres = 1 square mile (sq mi)

Volume

1,728 cubic inches = 1 cubic foot

27 cubic feet = 1 cubic yard (CU yd)

# **Counting Units**

12 units = 1 dozen (doz)

12 dozen = 1 gross

**144** units = **1** gross

24 sheets = 1 quire

480 sheets = 1 ream

#### **Equivalents**

1 cubic foot of water weighs 62.5 pounds (approx) = 1,000 ounces

1 gallon of water weighs 8-1/3 pounds (approx)

1 cubic foot = 7.48 gallons

1 inch = 2.54 centimeters

1 foot = 30.4801 centimeters

1 meter = 39.37 inches

1 liter = 1.05668 quarts (liquid) = 0.90808 quart (dry)

1 nautical mile = 6,080 feet (approx)

1 fathom = 6 feet

1 shot of chain = 15 fathoms

<b>F</b> 4	00040	
Feet	x.00019	= miles
Feet	x 1.5	= links
Yards	x .9144	= meters
Yards	x .0006	= miles
Links	x .22	= yards
Links	x .66	= feet
Rods	x 25	= links
Rods	x 16.5	= feet
Square inches	x .007	= square feet
Square inches	x 6.451	= square centimeters
Square centimeters	x 0.1550	= square inches
Square feet	x .111	= square yards
Square feet	x .0929	= centares (square meters)
Square feet	x 929	= square centimeters
Square feet	x 144	= square inches
Square yards	x .0002067	= acres
Acres	x 4840.0	= square yards
Square yards	x 1,296	= square inches
Square yards	x 9	= square feet
Square yards	x 0.8362	= centares
Square miles, statute	x 640	= acres
Square miles, statute	x 25,900	=ares
Square miles, statute	x 259	= hectares
Square miles, statute	x 2,590	= square kilometers
Cubic inches	x .00058	= cubic feet
Cubic feet	x .03704	= cubic yards
Tons (metric)	x 2,204.6	= pounds (avoirdupois)
Tons (metric)	x 1,000	= kilograms
Tons (short)	x 2,000	= pounds (avoirdupois)

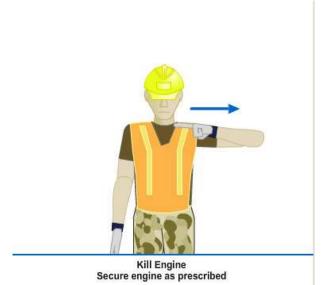
	I	I
Tons (short)	x 0.9072	= metric tons
Tons (long)	x 2,240	= pounds (avoirdupois)
Tons (long)	x 1.016	= metric tons
$\pi$	= 3.14592654	
1 radian	= 180°/ <i>π</i> = 57.2957790°	= approx. 57° 17' 44.8"
1 radian	= 1018.6 miles	
1 degree	= 0.0174533 radian	
1 minute	= 0.0002909 radian	
1 mil	= 0.0009817	
$\pi$ radians	= 180°	
$\pi$ /2 radians	= 90°	
Radius	= arc of 57.2957790°	
Arc of 1° (radius = 1)	= .017453292	
Arc of 1' (radius = 1)	= .000290888	
Arc of 1" (radius = 1)	= .000004848	
Area of sector of circle	= ½ Lr	(L= length of arc; r = radius)
Area of segment of parabola	= 2/3 cm	(c = chord; m = mid. ord.)
Area of segment of circle	= approx 2/3	
Arc – chord length	= 0.02 foot per 11 ½ miles	
Curvature of earth's surface	= approx. 0.667 foot per mile	

# **APPENDIX II**

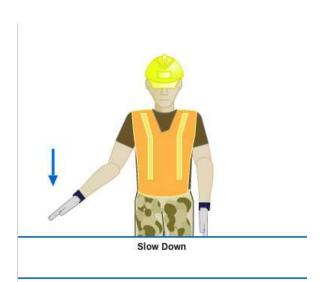
# **Hand Signals**



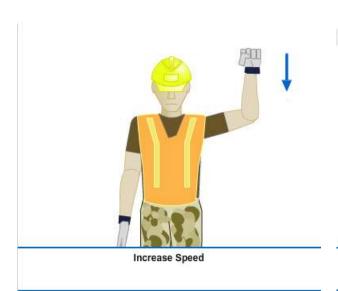














Raise Hoist Slowly Hurry up and move out, double time, etc.











Raise Boom

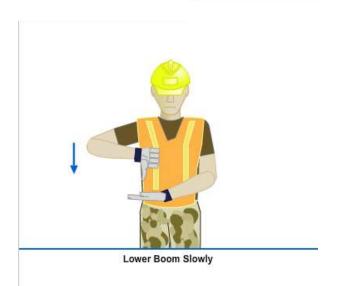




Raise Boom and Hold Load



Lower Boom and Hold Load



NAVEDTRA 14080A AII-4



Raise Boom Slowly



Lower Boom and Raise Load



Raise Boom and Lower Load



Swing In Direction Finger Points



Close Bucket



Open Bucket



Use Whip Line For Preceding Signals (Auxilliary Hoist) Tap elbow then use regular signals



Make Left Turn



Make Right Turn



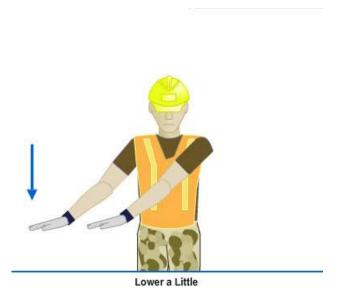
**Travel Both Tracks** 



Cut, Fill, or Drag Road Point to road to be dragged or bladed, then rub palms together. Applies to scrapers, motor graders, and bulldozers.



Raise a Little





Dump Load Now Start dumping and spreading load to proper depth if given.



Rehaul or Retract



Crowd or Extend







Turn Left (Operator's Left)

## **APPENDIX III**

# **COMMON CONSTRUCTION SYMBOLOGY**

Lighting Outlets		Switch Outlets		Annunciator	
Ceiling	Wall	Single-Pole Sw	itch	<b>~</b>	
Surface or Pendant In Mercury Vapor, or Sin			S	Interconnection Box	
0	-0		150		
Surface or Pendant In	dividual	Double-Pole Sw	riton		
Fluorescent Fixture			S2	Bell-Ringing Tranformer	
<u> </u>		Three-Way Swit	ch	BT	
Surface or Pendant C Individual Fluorescen			S3	Interconnecting Telephone	
CO. I		Four-Way Switc	:h	Ħ	
Bare Lamp Fluoresce	nt Strip	THE REAL PROPERTY.		Radio Outlet	
<del></del>	<del>-1 -1</del>		S4	R	
Surface or Pendant E	xit Light	Key-Operated S	Switch	STATE OF THE PROPERTY OF THE P	
Φ.	-0		Sĸ	Television Outlet	
Junction Box	(37/6	Switch and Pilo	t Lamp	TV	
Ø	<b>- 3</b>		SP	Panelboards, Switchboards, and	
Receptac	le Outlets	Switch for Low-Voltage Switching System		Related Equipment	
Grounded	Ungrounded	Switch for Low			
	12110 <del>2</del> 020010010000		SL	Flush-Mounted Panelboard and Cabinet	
Single Receptacle Ou	tlet	Switch and Sing	gle Receptacle	NOTE: Identify by notation or schedule	
<del>-0</del>	<b>→</b> 0386		- <del>O</del> s		
Duplex Receptacle Ou	utlet	Switch and Dou	ible Receptacle	20 20 20 20 20 20 20 20 20 20 20 20 20 2	
-⊕	<b>-⊕</b> 1382		<b>=</b> ⊕s	Surface-Mounted Panelboard and Cabinet	
Duplex Receptacle Ou		Door Switch			
-	<b>=</b> ⊕ mag		Sp	Switchboard, Power Control Center, Unit	
Single Special Purpos	se Receptacle Outlet	Time Switch		Substations (should be drawn to scale)	
-⊗	<b>-⊘</b> ‱	Time Switch	ST		
Range Outlet (typical)			0.	Florit Monated Tomologic Continue	
• • · · · ·	<b>■</b> COME	Pasidas	ntial Occupancies	Flush-Mounted Terminal Cabinet NOTE: In small-scale drawings the TC may	
Floor Duplex Recepta	cle Outlet	Resider	itiai Occupancies	be indicated alongside the symbol	
			m symbols for use in	TC	
Floor Telephone Outle	0.		dardized residential type tems on residential	Surface-Mounted Terminal Cabinet	
E			a descriptive symbol list	rc	
Application: example			**************************************	Motor or Other Power Controller	
symbols to identify lo types of outlets or co	cation of different	<b>Push Button</b>	•	HC	
underfloor duct or cel				Externally Operated Disconnection Switch	
(A)		Buzzer			
	6 2			0) <del></del>	
<b>⊚</b> ⊢	<b>∀e</b>	Bell	$\Box$	Combination Controller and Disconnection Means	
				<b>≥</b>	
911	⊕				

O eetlight O-X vn Guy and Anchor	Pole		Application:	ontrol Stations for Other Equipment	
eetlight O-X		3 wires; 4 wires; etc	<del>-////-</del>	tions in General	Push-button St
eetlight O-X			Unless indicated otherwise, th		
<u>•</u> α		required by	the circuit is the minimum size the specification.		Tl1 C
O-XX vn Guy and Anchor	Pole, with Streetli		Indicate size in inches and ide	시 <u>시(()</u> ()) (() () ()	Float Switch - N
vn Guy and Anchor			functions of wiring system, su signaling, by notation or other	[F]->	
vn Guy and Anchor		means.	Wiring Turned Up	echanical	Limit Switch - N
$\longrightarrow$	Pole, with Down 0				
$\hookrightarrow$		-0	<del>-</del>	ch - Mechanical	Pneumatic Swi
			Wiring Turned Down	₽⊢▶	
	Transformer	•			
A		•		am Source	Electric Eye - B
Δ				<b>¼</b> →	
Constant-Current	Transformer, Con			day	Electric Eye - R
			Manhole	nay:	Sectific Lye - IN
$\boldsymbol{\varphi}$			M	N .	
al .	Switch, Manual		Lim		Thermostat
	TOUR MANAGEMENT		Handhole	<del>-</del> ①	
<b>_</b> -	9		н		
er, Automatic	Circuit Recloser,		LH.		
			Transformer Pad	Circuiting	
R					
rv	Circuit, Primary		TP	dentification by notation specifications.	
ž	-	ole	Underground Direct Burial Ca	ed in Ceiling or Wall	
danu	Circuit, Secondar		Indicate type, size, and number	ever announce of the second	4
aary	on out, occording	edule.	conductors by notation or sch	weight line to identify	Note: Use heav
				runs	service and fee
Street Lighting	Circuit, Series Str			ed in Floor	Wiring Conceal
			Underground Duct Line		· — -
	Down Guy	e of duste	Indicate type, size, and number		
			by cross section identification		Wiring Exposed
			run by notation or schedule. I type, size, and number of con-		
	Head Guy	luctors by	notation or schedule.	lome Run to Panelboard	Branch Circuit
		204			
	Sidewalk Guy	_		vs indicates number of eral at each arrow may be	
048840	Sidewalk Gdy		Streetlight Standard Fed from	circuit number.)	
<b>→</b>			Underground Circuit	2 1	-
er Head	Service Weather I			uit without further	
^			У		
			~	N. N. 1994 (A. S. 1984 (1984) TANK AND 1987 (1984) (A. S. 1984) (A. S.	
er Head	Service Weather h		×	dicates a 2-wire circuit. mber of wires, indicate	dentification in

Qualifying Symbols

Connection Symbol

For use adjacent to other symbols

3-phase, 3-wire, delta

Δ

3-phase, 3-wire, delta, grounded

4

3-phase, 4-wire, delta, grounded



3-phase, open delta

L

3-phase, wye or star, ungrounded



3-phase, wye, grounded neutral



Graphic Symbols for Fundamental Items

Resistor

General



Application: adjustable or continuously adjustable (variable) resistor rheostat



NOTE: Always add identification within , or adjacent to, the rectangle. Capacitor



Antenna

General

Types or functions may be indicated by words or abbreviations adjacent to the symbol.



Battery

The long line is always positive, but polarity may be indicated in addition. Example:



Multicell



Thermal Element

Actuating device, self-heating or with external heater. (Not operated primarily by ambient temperature.)



Graphic Symbols for Transmission Path

Transmission Path Conductor Cable Wiring

Guided path, general

A single line represents the entire group of conditions or the transmission path needed to guide the power or signal.

When required, details of structure, type, impedance, ratings, etc., may be added adjacent to or within any symbol or in a note.

Busbar (with connections shown)
Use only if essential to distinguish bus
from other circuit paths.



Conductive path or conductor; wire

Two conductors or conductive paths

Crossing of paths or conductors not connected

The crossing is not necessarily at a 90° angle.



Junction of paths or conductors Junction (if desired)



Junction of paths, conductors, or cable. If desired, indicate path type, or size.



Junction of paths, conductors, or wires



2-conductor cable



Cable underground; underground line



These are long dashes

Overhead line



#### Circuit Return

#### Ground general symbol

NOTE: Supplementary information may be added to define the status or purpose of the earth if this is not readily apparent.

- A direct conducting connection to the earth or body of water that is a part therof.
- (2) A conducting connect to a structure that serves a function similar to that of an earth ground (that is, a structure such as a frame of an air, space, or land vehicle that is not conductively connected to earth)



Chassis or frame connection, equivalent chassis connection (of printed-wiring boards)

A conducting connection to a chassis of frame (or equivalent chassis connection of a printed-wiring board) may be at substantial potential with respect to the earth or structure in which this chassis or frame (or printed-wiring board) is mounted.



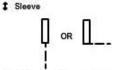
Graphic Symbols for Contacts, Switches, Contacts, and Relays

#### Electrical Contact

Fixed contact for jack, key, relay, switch, etc.



====



The broken line --- indicates where line connection to a symbol is made and is not part of the symbol.

#### **Moving Contact**

Adjustable or sliding contact for resistor, inductor, etc.



Locking



Nonlocking



#### **Basic Contact Assemblies**

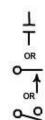
The standard method of showing a contact is by a symbol indicating the circuit condition it produces when the actuating device is in the de-energized or nonoperated position. The actuating device may be of a mechanical, electrical, or other nature, and a clarifying note may be necessary with the symbol to explain the proper point at which the contact functions; for example, the point where a contact closes or opens as a function of changing pressure, level, flow, voltage, current, etc. In cases where it is desirable to show contacts in the energized or operated condition and where confusion may result, a clarifying note shall be added to the drawing.

#### Closed contact (break)

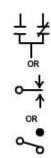




#### Open contact (make)



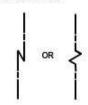
#### Transfer



#### Make-before-break



#### Magnetic Blowout Coil



Operating Coil Relay Coil



### Switch

Fundamental symbols for contacts, mechanical connections, etc, may be used for switch symbols.

Single-throw, general



Double-throw, general



2-pole double-throw switch with terminals shown



NOTE: The asterisk is not part of the symbol. Always replace the asterisk by a device designation.

Push button, Momentary or Spring-Return

Circuit closing (make)



Circuit opening (break)



Two-circuit



Selector or Multiposition Switch

The position in which the switch is shown may be indicated by a note or designation of switch position.

General (for power and control diagrams)

Any number of transmission paths may be shown.



OR



Limit Switch Sensitive Switch

NOTE: Identity by LS or other suitable note.

Track-type, circuit-closing contact



Track-type, circuit-opening contact



Flow-Actuated Switch

Closes on increase in flow



Opens on increase in flow



Liquid-Level-Actuated Switch

Closes on rising level



Opens on rising level



Pressure-or Vacuum-Actuated Switch

Closes on rising pressure



Opens on rising pressure



Temperature-Actuated Switch

Closes on rising temperature



Opens on rising temperature



Thermostat

Closes on rising temperature



Contactor

See also CIRCUIT BREAKER

Fundamental symbols for contacts, coils, mechanical connections, etc, are the basis of contactor symbols and should be used to represent contactors on complete diagrams. Complete diagrams of contactors consist of combinations of fundamental symbols for control coils, mechanical connections, etc, in such configurations as to represent the actual device. Mechanical interlocking should be indicated by notes.

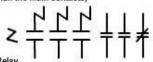
Manually operated 3-pole contactor



NOTE: The t<sup>a</sup> symbol shall be shown or be replaced by data giving the nominal or specific operating temperature of the device. Electrically operated 1-pole contactor with series blowout coil

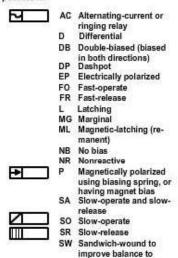


Electrically operated 3-pole contactor with series blowout coils; 2 open and 1 closed auxiliary contacts (shown smaller than the main contacts)



Fundamental symbols for contacts, mechanical connections, colls, etc, are the basis of relays on complete diagrams.

The following letter combinations or symbol elements may be used with relay symbols. The requisite number of these letters or symbol elements may be used to show what special features a relay possesses.

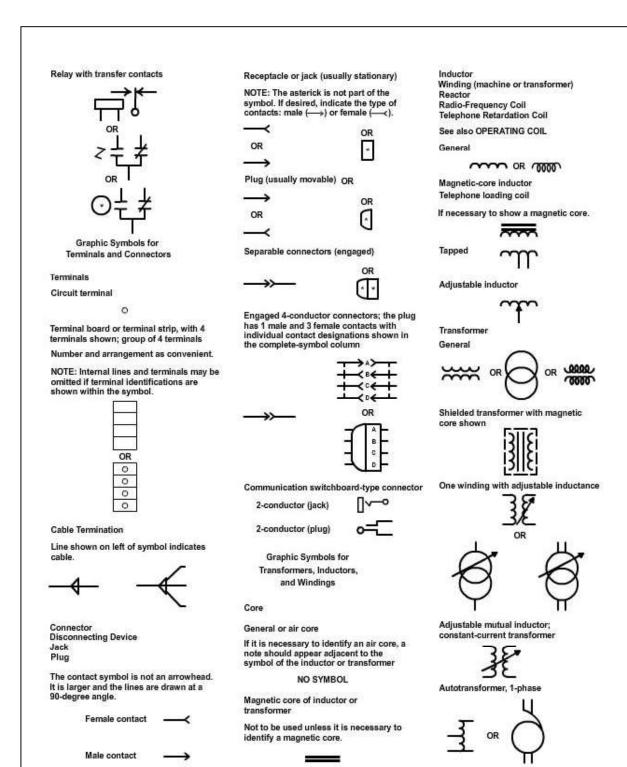


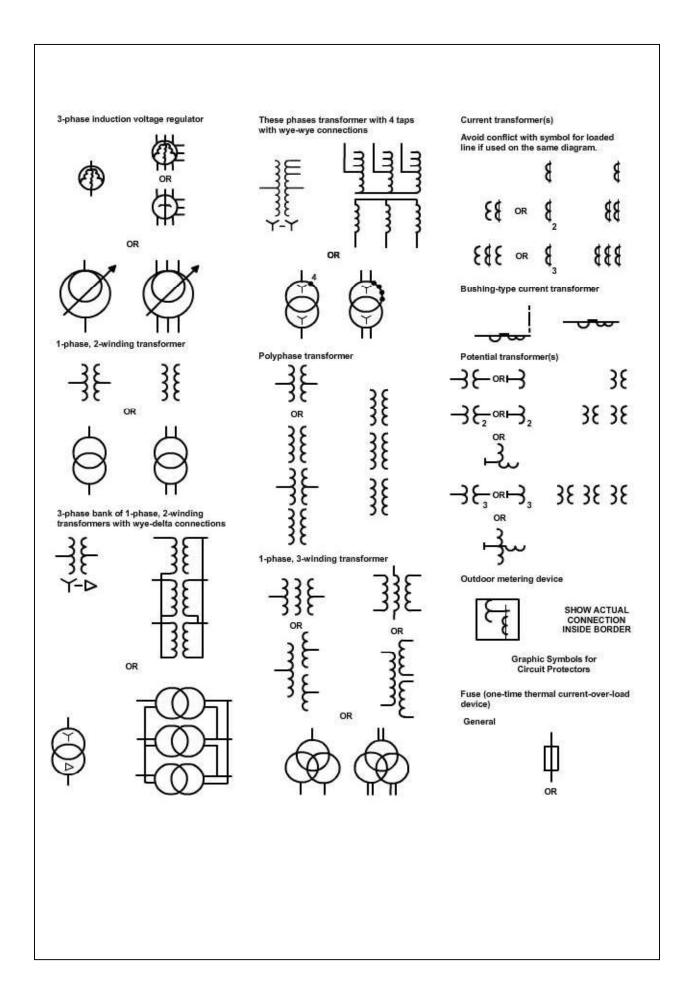
Iongitudinal currents
The proper poling for a polarized relay shall be shown by the use of + and - designations applied to the winding leads. The interpretation of this shall be that a voltage applied with the polarity as indicated shall cause the armature to move toward the contact shown nearer the coil on the diagram. If the relay is equipped with numbered terminals, the proper terminal numbers shall alson be shown.

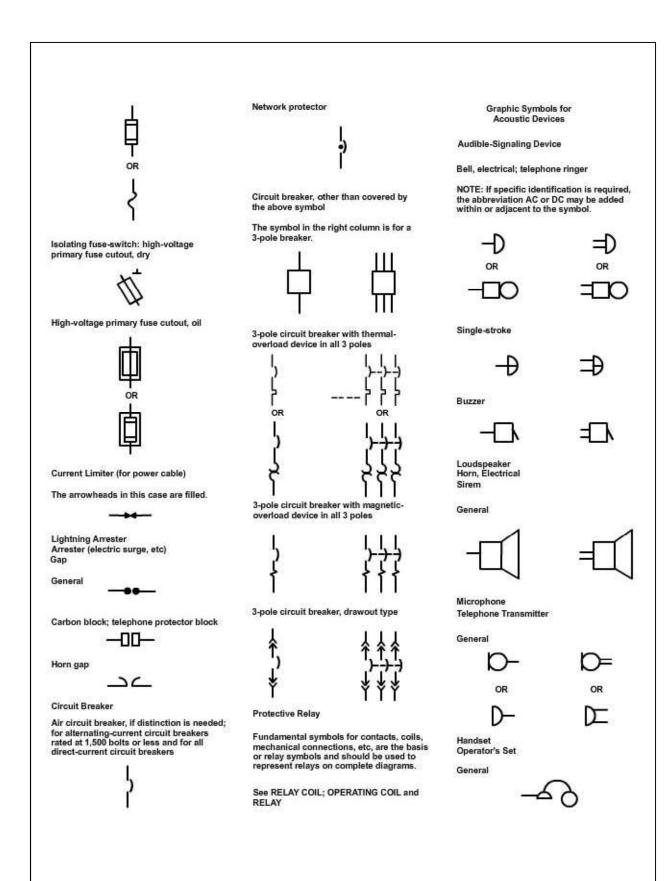
Basic



NAVEDTRA 14080A





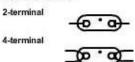


Telephone Receiver Earphone General Headset, double Headset, single Graphic Symbols for Lamps and Visual-Signaling Devices Lamp Lamp, general; light source, general Amber

NOTE: This symbol may be used to represent one or more lamps with or without operating auxiliaries NOTE: If it is essential to indicate the following characteristics, the specified letter or letters may be inserted within or placed adjacent to the symbol. Blue C Clear G Green 0 Orange OP P Opelescent Purple Red

R White Yellow ARC Arc EL Electroluminescent FL Fluorescent HG Mercury vapor IN Incandescent IR Infrared NA Sodium vapor NF Neon Ultraviolet UV XE Xenon Light-emitting diode

Fluorescent lamp



Incandescent lamp (incandescent-filament illuminating lamp



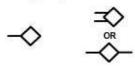
Ballest lamp; ballast tube

The primary characteristic of the element within the circle is designed to vary non-linearity with the temperature of the



Visual-Signaling Device

Annunciator (general)



Annunciator drop or signal, shutter or grid type



Annunciator drop or signal, ball type



Manually restored drop



Electrically restored drop



Communication switchgoard-type lamp; indicating lamp



Indicating, pilot, signaling, or switchboard light; indicator light signal light

If confusion with other circular symbols may occur, the D-shape symbol should







Jeweled signal light



Graphic Symbols for Readout Devices

Meter Instrument

NOTE: The asterisk is not part of the symbol. Always replace the asterisk by one of the following letter combinations, depending on the function of the meter or instrument, unless some other identification is provided in the circle and explained on the diagram.



	$\odot$
A	Ammeter
AH	Ampere-hour meter
C	Coulombmeter
CMA	Contact-making (or breaking)
CMC	ammeter Contact-making (orbreaking) clock
CMV	Contact-making (or breaking) voltmeter
CRO	Oscilloscope Cathode-ray oscillograph
DB	DB (decibel) meter Audio level/meter
DBM	DBM (decibels referred to 1 milliwatt) meter
DM	Demand meter
DTR	Demand-totalizing relay
F	Frequency meter
GD	Ground detector
I .	Indicating meter
µ A or UA	
MA	Milliammeter
NM	Noise Meter
OHM	Ohmmeter
OP	Oil pressure meter
OSCG	Oscillograph
PF	Power factor meter
PH	Phasemeter
PI	Position indicator
RD	Recording demand meter
REC	Recording meter
RF	Reactive factor meter
SY	Synchroscope Temperature meter
THC	Thermal converter
TLM	Telemeter
П	Total time meter
33	Elapsed time meter
V	Voltmeter
VA	Volt-ammeter
VAR	Varmeter
VARH	Varhour meter
VI	Volume indicator
2000	Audio-level meter
VU	Standard volume indicator

Audio-level meter

Watthour metery

Wattmeter

W

WH

3-phase wye (ungrounded) Graphic Symbols for Galvanometer Mechanical Functions Mechanical Connection Mechanical Interlock 3-phase wye (grounded) Mechanical connection Graphic Symbols for The top symbol consists of shor dashees. Rotating Machinery NOTE: The short parallel lines should be used only where there is insufficient space for the short dashes in series Rotating Machine 3-phase delta OR Generator (general) **Alternating-Current Machines** Mechanical Motion Squirrel-cage induction motor or generator, split-phase induction motor or Avoid conflict with symbols for galvanogenerator, rotary phase converter, or repulsion motor Translation, one direction meter if used on the same diagram. Translation, both directions Generator, direct-current Wound-rotor induction motor, synchronous induction motor, induction generator, or Rotation, one direction induction frequency converter Generator, alternating-current Application: angular motion, applied to open contact (make), symbol 1-phase shaded-pole motor Motor (general) NOTE: The asterisk is not part of the symbol. Explanatory information (similar to type shown) may be added if neccessary to explain circuit operation. 1-phase repulsion-start induction motor Motor, direct-current 3-phase regulating machine Motor, alternating-current Rotation, both directions Winding Connection Symbols Motor and generator winding connection Alternating-Current Machines with symbols may be shown in the basic circle using the following representations. **Direct-Current Field Excitation** Alternating or reciprocating 1-phase Synchronous motor, generator, or condensery Rotation designation (applied to a resistor) CW indicates position of adjustable contact 2-phase at the limit of clockwise travel viewed from knob or actuator end unless otherwise

NOTE: The asterisk is not part of the symbol. Always add identification within or adjacent to the rectangle.



Manual Control

General



Operated by pushing



Operated by pushing and pulling (pudh-pull)



Graphic Symbols for Composite Assemblies

Circuit Assembly Circuit Subassembly Circuit Element

NOTE: The asterisk is not part of the symbol. Always indicate the type of apparatus by appropriate words or letters.

NOTE: The use of a general circuitelement symbol is restricted to the following:

- a. Diagrams drawn in block form.
- A substitute for complex circuit elements when the internal operation of the circuit element is not important of the purpose of the diagram.

General



Accepted abbreviations from ANSI Z32.13-1950 may be used in the rectangle.

The following letter combinations may be used in the rectangle:

CLK Clock
EQ Equalizer
FAX Facsimile set
FL Filter

IND Indicator Power supply PS RG Recording unit Reproducing unit RU Telephone dial DIAL Telephone station TEL Teleprinter TPR Teletypewriter TTY

Amplifier

General

The triangle is pointed in the direction of transmission.

The symbol represents any method of amplification (electron tube, solid-state device, magnetic device, etc).

NOTE: If identification, electrical values, location data, and similar information must be noted within symbol, the size or aspect ratio of the original symbol may be altered providing its distinctive shape is retained.

Amplifier use may be indicated in the triangle by words, standard abbreviations, or a letter combination from the following list:

BOG Bridging BST Booster CMP Compression EXP Direct-current Limiting LIM MON Monitoring PGM Program Preliminary PRE PWR Power TRO Torque





Application: amplifier with associated power supply





General

NOTE: Triangle points in direction of forward (easy) current as indicated by a direct-current ammeter, unless otherwise noted adjacent to the symbol. Electron flow is in the opposite direction. NOTE: This symbol represents any method of rectification (electron tube, solid-state device, electrochemical device, etc).



Controlled



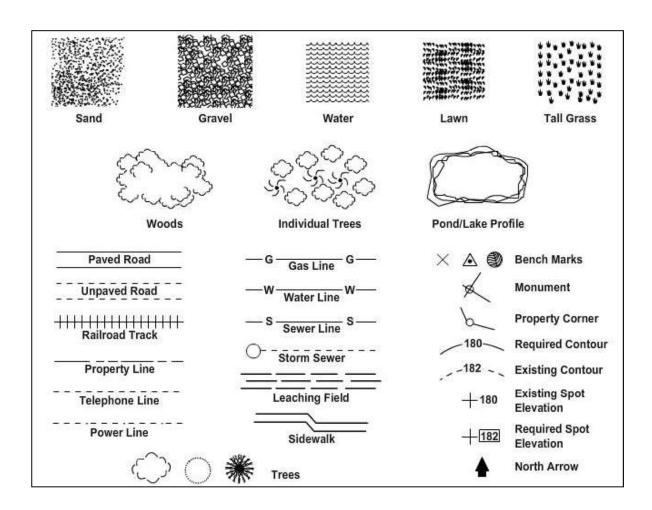
Bridge-type rectifier



On connection or wiring diagrams, rectifier may be shown with terminals and plarity marking. Heavy line may be used to indicate nameplate or positive-polarity end.



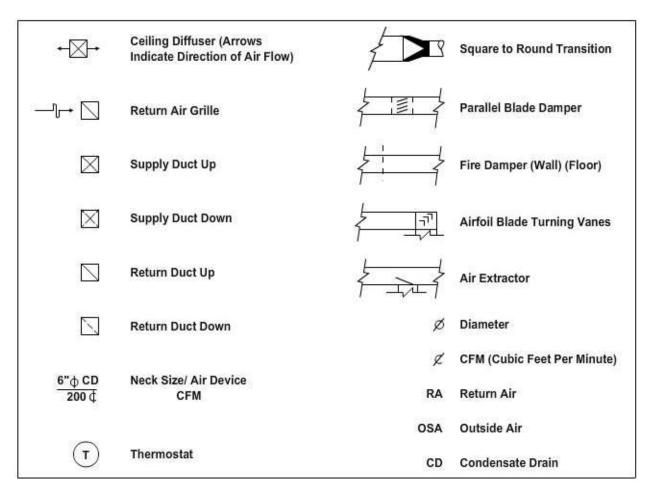
For connection or wiring diagram

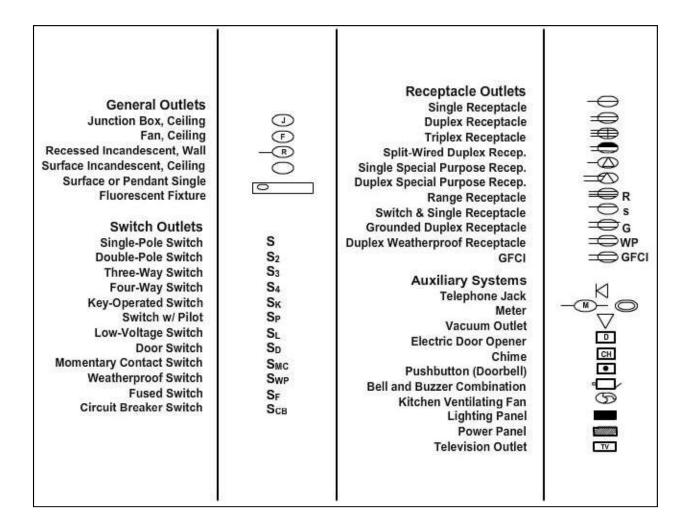


Description	Example	Symbol	Illustrated Use
W- Shape (Wide Flange)	56	w	W24 x 78
Bearing Pile	<u>-</u>	BP	BP14 x 73
S-Shape (American STD I-Beam)	Ø	s	S15 x 42.9
C-Shape (American STD Channel)	<u> </u>	С	C9 x 13.4
M-Shape (Misc Shapes Other Than W, BP, S, & C)		м	M5 x 34.3
W, BF, 3, & C)			M5 x 17
		585500	M7 x 5.5
MC-Shape (Channels Other Than American STD)		MC	MC12 x 45 MC 12 x 12.8
Angles:	1		3x 3x
Equal Leg		L	L 3x 3x 1/4
Un-equal Leg	6	L	L 7x 4x 1/2
Tees, Structural: Cut From W-Shape	7	WT	WT 12x38
Cut From S-Shape	IV.	ST	ST 12x38
Cut From M-Shape		MT	MT 12x38
Plate		PL	PL 1/2x18"x30"
Flat Bar		BAR	BAR 2 1/2 x 1/4
Pipe, Structural		10270101000 FC	Pipe 4 STD
- Parameter		<b>(</b>	Pipe 4x-STRG
	922-	4	Pipe XX-STRG

0	BASIC WELD SYMBOLS								
		PLUG	GROOVE OR BUTT						
BEAD	FILLET	OR SLOT	SQUARE	٧	BEVEL	U	J	FLARE V	FLARE BEVEL
	7		11	<	/	$\left\langle \cdot \right\rangle$	Y	7	1

	CONTOUR		WELD-	FIELD WELD	
FLUSH	CONVEX	CONCAVE	ALL-AROUND		
<u></u>	<u>~</u>	~	<i>&gt;</i>		





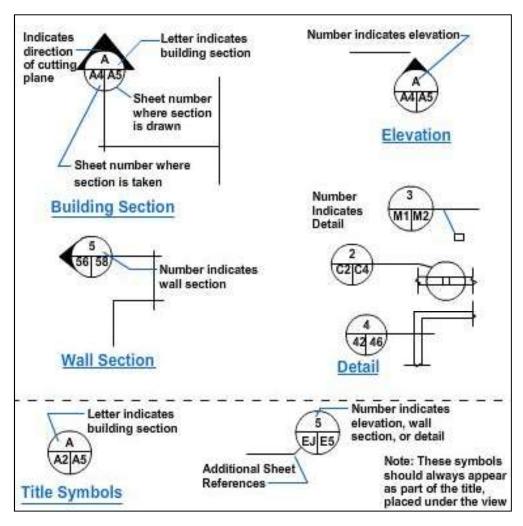
Plumbing	
Corner Bath	
Recessed Bath	
Roll Rim Bath	
Sitz Bath	
Floor Bath	
Bidet	
Shower Stall	ाजा ह्या
Shower Head	
Overhead Gang Shower	(LPH -0-0-0
Pedestal Lavatory	Chet III
Wall Lavatory	
Corner Lavatory	
Manicure Lavatory	9800.3019
Medical Lavatory	
Dental Lavatory	<u> </u>
Plain Kitchen Sink	
Kitchen Sink, R & L Drain Board	<b>I</b> II
Kitchen Sink, L H Drain Board	💷
Combination Sink and Dishwasher	
Combination Sink & Laundry Tray	(7.5.50
Service Sink	스타이트 교육하다 어때를 하고 특별하
Wash Sink (Wall Type)	
Wash Sink	[000]
Laundry Tray	<u></u>
Water Closet (Low Tank)	
Water Closet (No Tank)	Ō
Urinal (Pedestal Type)	⊖
Urinal (Wall Type)	
Urinal (Corner Type)	<i>D</i>
Urinal (Stall Type)	
Urinal (Trough Type)	
Drinking Fountain (Pedestal Type)	
Drinking Fountain (Wall Type)	v
Drinking Fountain (Trough Type)	- Бұн
Hot Water Tank	①
Water Heater	
Meter	ю́н
Hose Rack	
Hose Bibb	∓
Gas Outlet	Ţ
Vacuum Outlet	·
Drain	📮
Grease Separator	
Oil Separator	
Cleanout	
Garage Drain	
Floor Drain With Backwater Valve	
Roof Sump	0

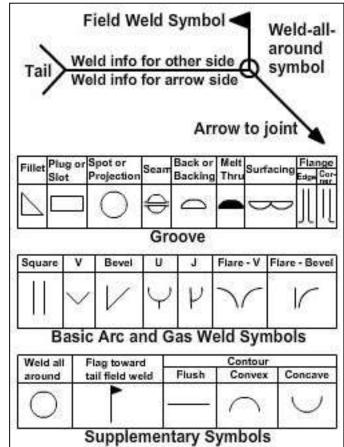
		LINE STANDARDS	
Name	Convention	Description and Application	Example
Center Lines		Thin lines made up of long and short dashes alternately spaced and consistent in length.  Used to indicate symmetry about an axis and location of centers.	<b>\$</b>
Visible Lines		Heavy unbroken lines Used to indicate visible edges of an object	
Hidden Lines		Medium lines with short evenly spaced dashes Used to indicate concealed edges	
Extension Lines		Thin unbroken lines Used to indicate extent of dimensions	-
Dimension Lines	1	Thin lines terminated with arrow heads at each end  Used to indicate distance measured	
Leader	1	Thin line terminated with arrowhead or dot at one end  Used to indicate a part, dimension or other reference	1/4 × 20 UNC THD.
Break (Long)		Thin, solid ruled lines with freehand zigzags  Used to reduce size of drawing required to delineate object and reduce detail	
Break (Short)	3	Thick, solid free hand lines Used to indicate a short break	<u> </u>
Phantom or Datum Line		Medium series of one long dash and two short dases evenly spaced ending with long dash  Used to indicate alternate position of parts, repeated detail or to indicate a datum plane	
Stitch Line		Medium line of short dases evenly spaced and labeled Used to indicate stitching or sewing	Sti
Cutting or Viewing Plane Viewing Plane Optional	<u>†</u> †	Thick solid lines with arrowhead to indicate direction in which section or plane is viewed or taken	<b>t</b> ⊕
Cutting Plane for Complex or Offset Views	***	Thick short dashes  Used to show offset with arrowheads to show direction viewed	

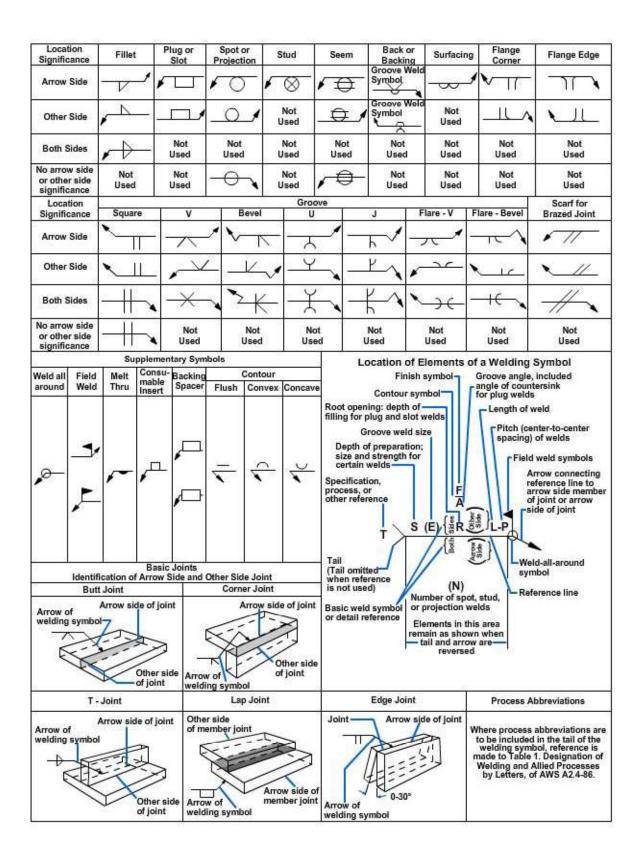
Screwed Soldered
→◆ →◆
ᠯ⊶
64
······································
}- }-
⊣a⊢ –)a⊢
₩- ₩

	rewed Solderes
Joint	+ +
Elbow - 90	f + +>
Elbow - 45	X X
Elbow - Turned Up	o <del>⊢</del> o⊢
Elbow - Turned Down	>+ O+
Elbow Long Radius	Æ.
Side Outlet Elbow-	AF 40
Outlet Down	f' '¥
Side outlet Elbow -	P+ +9
Outlet Up	1 1
Base Elbow	# t+
Double Branch Elbow d	<b>*</b>
Single Sweep Tee	7
Double Sweep Tee	<del>'Y'</del>
Reducing Elbow	<u>^</u>
Tee	† †
Foo Outlet UD	+++ <del>++</del> +
Tee - Outlet Down	<del>0</del> <del>0</del>
Side Outlet Tee -	ĭ
Outlet up	O+ +O+
Side Outlet Tee - Outlet Down	4
Cross	<del>↓</del> + <del>}</del>
Reducer	OH - OH
Eccentric Reducer	X X
_ateral	t t
Expansion Joint Flanged	<del>+</del> <del>+</del>

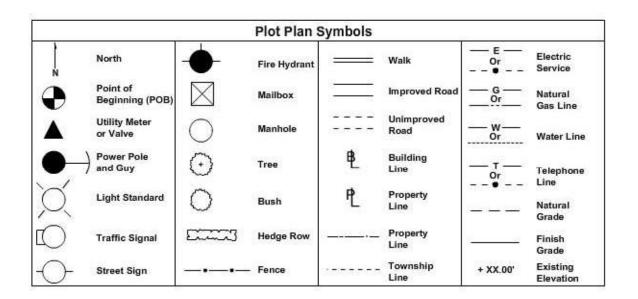
	Battery, Multicells	F	Fire-Alarm Box, Wall Type	s	Single-Pole Switch
-00 10A	Switch Breaker		Lighting Panel	S <sub>2</sub>	Double-Pole Switch
30A	Automatic Reset Breaker		Power Panel	3	Pull Switch Ceiling
¥ <del>p</del> d‡	Bus	ÿ <del>s</del>	Branch Circuit, Concealed In Ceiling Or Wall	-(3)	Pull Switch Wall
ூ	Voltmeter	·	Branch Circuit, Concealed In Floor	8	Fixture, Fluorescent, Ceiling
-0'0-	Toggle Switch DPST	of <u>Bearing teaching</u>	Branch Circuit, Exposed	-8	Fixture, Fluorescent, Wall
	Transformer, Magnetic Core	<u> </u>	Feeders	0	Junction Box, Ceiling
	Bell	≡□≡	Underfloor Duct And Junction Box	-0	Junction Box, Wall
ÁC II	Buzzer, AC	M	Motor	©	Lampholder, Ceiling
+	Crossing Not Connected (Not Necessarily At A 90° Angle)	$\boxtimes$	Controller	<u>-</u> Q	Lampholder, Wall
+	Junction	×	Street Lighting Standard	C <sub>Ps</sub>	Lampholder, With Pull Switch, Ceiling
	Transformer, Basic	•	Outlet, Floor	O <sub>PS</sub>	Lampholder, With Pull Switch, Wall
Ť	Ground	$\Rightarrow$	Convenience, Duplex	$\bigcirc$	Special Purpose
0	Outlet, Ceiling	-0	Fan, Wall	M	Telephone, Switchboard
-0	Outlet, Wall	(F)	Fan, Ceiling	<del>-</del> ①	Thermostat
	Fuse	111	Knife Switch Disconnected	•	Push Button

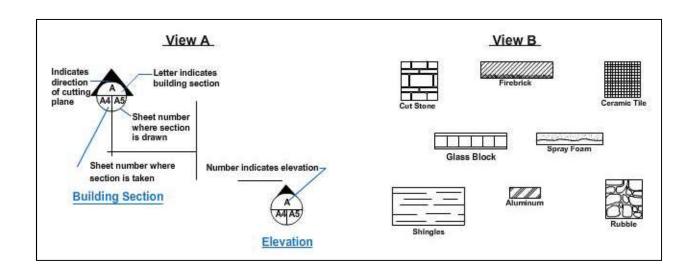




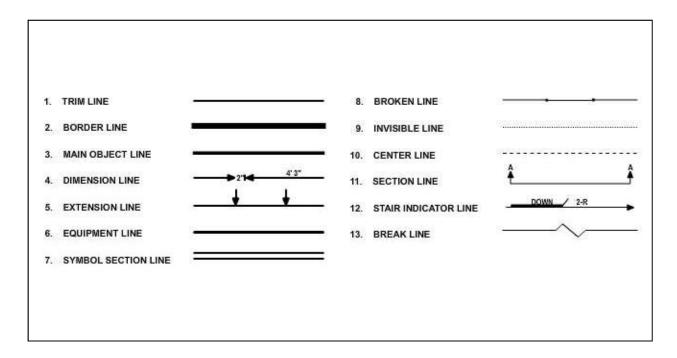


	Arch	itectural Symbols	
Material	Elevation	Plan	Section
Earth			
Brick	With note indicating type of brick (common, face, ets.)	Common or Face Firebrick	Same as Plan Views
Concrete		Lightweight	Same as Plan Views
Concrete Block		771.11	Or 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2
Stone	Cut Stone Rubble	Cut Stone Rubble  Cast Stone (Concrete)	Cut Stone Cast Stone Rubble or Cut Stone
Wood	Siding Panel	Wood Stud Display  Remodeling	Rough Finished Plywoo
Plaster		Wood Stud, Lath, Metal Lath, and Plaster and Plaster	Lath and Plaster
Roofing	Shingles	Same as Elevation View	7074 ( 7707
Glass	Or Glass Block	Glass Glass Block	Small Large Scale Scale
Facing Tile	Ceramic Tile	Floor Tile	Ceramic Tile Ceramic Tile Large Scale Small Scale
Structural Clay Tile			Same as Plan Views
Insulation		Loose Fill or Batts Rigid Spray Foam	Same as Plan Views
Sheet Metal Flashing		Occasionally Indicated by Note	
Metals Other Than Flashing	Indicated by Note or Drawn to Scale	Same as Elevation	Steel Cast Iron  Small Aluminum Bronze or Bras
Structural Steel	Indicated by Note or Drawn to Scale	Or	LI Rebars Large Scale L-Angles, S-Beams, etc.





Contours	21-
Depression Contour	
Stream	
Boundary or Right-of-Wa	y Line ————
Paved Road	
Unpaved or Gravel Road	:::::::::::::::::::::::::::::::::::::::
Trail	=======================================
Walk	Туре
Railroad	***************************************
Abandoned Railroad	****** ***** ***
Tunnel	>=====
Bridge	$\geq$
Box Culvert	_sīzē □
Pipe Culvert	
Dams	117 7/5
Retaining Wall	Туре
Bulkhead	Type
Pier	Туре
Fence	××
Hedge	www
Canal or Ditch	Canal
Marsh	34 M 34
Woods	(E.E.E.E.E.E.E.E.E.E.E.E.E.E.E.E.E.E.E.
Individual Trees	(E3)
Shoreline	- Sept
Depth Curve	8



Leader, Soil, or Waste (Above Grade)	(d)
(Below Grade)	
Vent	
Cold Water	
Hot Water	
Hot-Water Return	
Drinking Water	2-39-39-39-39-39-39-39-39-39-39-39-39-39-
Drinking Water Return	7 <del>. (</del>
Acid Waste	ACID
Compressed Air	— A —— A —
Fire Line	— F —— F —
Gas Line	— G —— G —
Tile Pipe	<u> — т — т —</u>
Vacuum	— v —— v —

